# The Crystal Structure of Cyclooctatetraenecarboxylic Acid ${ }^{1}$ 

David P. Shoemaker, Hubert Kindler, ${ }^{2}$ William G. Sly, and Ramesh C. Srivast ava<br>Contribution from the Department of Chemistry, Massachusetts Institute of Technology, Cambridge, Massachusetts. Received October 19, 1964

The crystal structure of 1,3,5,7-cyclooctatetraenecarboxylic acid has been determined by X-ray diffraction analysis. The crystals are monoclinic, space group $C_{2 h^{5}}-P 2_{1} / c$ (with $a_{0}=6.76, b_{0}=14.64$, and $c_{0}=8.37$ $\AA . ; \beta=110^{\circ} 9.5^{\prime}$ ) and the unit cell contains four molecules. The cyclooctatetraene ring is tub form, conforming closely to the $D_{2 d}$ symmetry found by gas phase electron diffraction work. The mean double-bond and single-bond distances in the ring are 1.322 and $1.470 \AA$., respectively, with estimated standard deivations of 0.005 $A .$, and the mean interbond angle in the ring is $126.4^{\circ}$, with an e.s.d. of $0.4^{\circ}$. The molecules are present as hydrogen-bonded dimers, with an $O-H \cdots O$ distance of $2.604 \AA$.

## Introduction

This study of the crystal structure of $1,3,5,7$-cyclooctatetraenecarboxylic acid ${ }^{3}$ (hereinafter referred to as


COT acid) was undertaken in 1952 in view of the then current interest and controversy concerning the shape of the cyclooctatetraene (COT) ring in the hydrocarbon itself. That controversy is now history; notwithstanding infrared and Raman spectroscopic evidence adduced for a crown configuration of $D_{4}$ symmetry in the vapor state, ${ }^{4}$ there now seems to be little doubt that a "tub" configuration of $\mathrm{D}_{2 d}$ symmetry with alternating single and double bonds is the correct one. This has been shown by electron diffraction studies in the vapor state $^{5-7}$ and by X-ray diffraction studies in the solid state. ${ }^{8}$ Our early results for COT acid ${ }^{9}$ showed indeed that the COT ring in this compound has the "tub" configuration.

Refinement of this structure took place sporadically over an unusually long period. It is now as complete

[^0]as could reasonably be desired and the results are reported here.

## Experimental

A sample of COT acid was kindly provided by Professor A. C. Cope. Crystals, grown by sublimation onto the walls of a test tube, were in the form of monoclinic plates or laths perpendicular to the $b$ axis and

Table I. Atomic Positional Coordinates

| -Atom—— |  | $\begin{aligned} & X \\ & Y \end{aligned}$ | $\sigma \times 10^{5}$ | Final shift $\times 10^{5}$ |
| :---: | :---: | :---: | :---: | :---: |
| No. | Kind | $Z$ |  |  |
| 1 | C(1) | 0.23518 | 58 | 5 |
|  |  | 0.19092 | 26 | -15 |
|  |  | 0.42007 | 48 | -2 |
| 2 | C(2) | 0.44308 | 68 | -2 |
|  |  | 0.19468 | 27 | -5 |
|  |  | 0.46905 | 57 | 5 |
| 3 | C(3) | 0.56964 | 68 | -9 |
|  |  | 0.26831 | 34 | -16 |
|  |  | 0.43536 | 60 | 0 |
| 4 | C(4) | 0. 56371 | 74 | $-16$ |
|  |  | 0.35525 | 32 | 9 |
|  |  | 0.47711 | 69 | 18 |
| 5 | C(5) | 0.43044 | 82 | 9 |
|  |  | 0.39593 | 30 | -20 |
|  |  | 0.56145 | 68 | 7 |
| 6 | C(6) | 0.22139 | 87 | 8 |
|  |  | 0.39340 | 27 | 8 |
|  |  | 0.51120 | 69 | 8 |
| 7 | C(7) | 0.08106 | 69 | 35 |
|  |  | 0.34704 | 29 | -3 |
|  |  | 0.35493 | 64 | -25 |
| 8 | C(8) | 0.08733 | 62 | -25 |
|  |  | 0.26045 | 29 | 3 |
|  |  | 0.31732 | 53 | 19 |
| 9 | C(9) | 0.13403 | 62 | -9 |
|  |  | 0.10704 | 24 | -15 |
|  |  | 0.45367 | 51 | -2 |
| 10 | $\mathrm{O}(1)$ | -0.06329 | 48 | -1 |
|  |  | 0.10006 | 20 | -6 |
|  |  | 0.40268 | 47 | -1 |
| 11 | $\mathrm{O}(2)$ | 0.25589 | 48 | -23 |
|  |  | $0.04298$ | 20 | 1 |
|  |  | 0.53736 | 50 | 21 |
|  |  | Hydrogen positions |  |  |
|  | Atom | $X$ | Y | $Z$ |
|  | H(2) | 0.5377 | 0.1394 | 0.5416 |
|  | H(3) | 0.6743 | 0.2459 | 0.3706 |
|  | H(4) | 0.6657 | 0.4042 | 0.4475 |
|  | H(5) | 0.5192 | 0.4314 | 0.6771 |
|  | H(6) | 0.1377 | 0.4263 | 0.5843 |
|  | H(7) | -0.0341 | 0.3920 | 0.2695 |
|  | H(8) | -0.0217 | 0.2336 | 0.2004 |
|  | H | 0.1624 | $-0.0040$ | 0.5486 |

with the longest direction parallel to $c$, showing good (001) cleavage. Crystals or cleaved fragments were mounted on glass fibers and reduced to cylinders about 0.2 mm . in diameter by rotating them incontact with filter

Table II. Anistropic Thermal Parameters ${ }^{a}$

${ }^{a}$ Values of $U_{i}$, the r.m.s. vibrational amplitudes, are given in Ånstrøm units. The direction cosines, $u$, $v$, and $w$, are taken with respect to a set of Cartesian coordinates with the $X^{\prime}$ axis codirectional with $a$, the $Y^{\prime}$ axis codirectional with $b$, and the $Z^{\prime}$ axis making an angle of $20^{\circ}$ $9.5^{\prime}$ with $c$. Thus in Figure 2, the $X^{\prime}$ and $Y^{\prime}$ axes lie in the plane of the paper and the $Z^{\prime}$ axis comes perpendicularly out of the paper.
paper moistened with alcohol. Lattice constants were determined by means of $\mathrm{Cu} \mathrm{K} \alpha$ rotation photographs, with NaCl powder lines on them for calibration. The values obtained were $a_{0}=6.76 \pm 0.01, b_{0}=14.64 \pm$ 0.02 , and $c_{0}=8.37 \pm 0.01 \AA . ; \beta=100^{\circ} 9.5^{\prime} \pm$ $5^{\prime}$. These values lead to a calculated density of 1.255 g. $\mathrm{cm} .^{-3}$ on the assumption of four 'molecules per unit cell; the observed density is $1.256 \pm 0.005 \mathrm{~g} . \mathrm{cm} .^{-3}$ by flotation in heptane-carbon tetrachloride mixtures. The absence of ( $0 k 0$ ) reflections with $k$ odd and of ( $h 0 l$ ) with $l$ odd indicated the space group $\mathrm{C}_{2 \mathrm{~h}}{ }^{5}-\mathrm{P}_{1} / \mathrm{c}$. Intensity data for about 1650 planes were obtained by visual estimation with calibrated film strips from multiple-film equi-inclination Weissenberg photographs taken with copper $\mathrm{K} \alpha$ radiation. No absorption corrections were made.

## Determination of the Structure

The structure was solved with a three-dimensional Patterson function, consisting of sections computed on the analog computer XRAC at Pennsylvania State University. A reasonably well resolved peak about $2.25 \AA$. from the origin was ascribed to the $\mathrm{O} \cdots \mathrm{O}$
intracarboxyl vector. With the use of required relations among peak positions for non-Harker and Harker peaks, it was possible to assign positions to the two oxygen atoms in the asymmetric unit. These positions, with their symmetry equivalents, were used as origins of eight shifted Patterson functions in an objective "Patterson superposition" or "vector convergence" procedure. ${ }^{10}$ Carbon atoms were taken to be at positions where all eight shifted Patterson functions were above a preselected minimum value. Only two such positions were found in the asymmetric unit that could not reasonably be interpreted as atom positions; these were assumed to result from accidental congruences. The other nine, with the two oxygen positions first found, defined a chemically reasonable COT acid molecule with a tub-form COT ring.

The structure was refined by least squares. ${ }^{11}$ The initial refinement was done on an IBM 704 computer with program NYXRI. ${ }^{12}$ Unit weights were used, off-diagonal normal equation matrix elements were
(10) C. A. Beevers and J. M. Robertson, Acta Cryst., 3, 164 (1950).
(11) E. W. Hughes, J. Am. Chem. Soc., 63, 1737 (1941).
(12) Program NYXR1 was written by D. Sayre, IBM Company. We used a modification made by V. Vand, Pennsylvania State University.

| ᄂ FOBS FCA | 4 fors F | foes PCal | Pots | Obs fcal | FOBS FCAL | OBS | ObS fCAL | fobs fcal | 08 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bigcirc 06$ | 8 9 60x | $7{ }^{22}{ }^{26}$ | 17 L | 13 | $-9$ | 12 | 31 | 33 L |  |
| ${ }^{2} 8933^{1228 x}$ | 010 - |  |  |  | $\begin{array}{lll}-8 & 9 & -1 * \\ & 39 & \\ -7 & 39 & -35\end{array}$ |  | ${ }^{2} 3218140$ | 0 | 29-26 |
| - 96 | ${ }^{4}$ | 12 L |  | -6 33 -33 <br> -3 16  <br>  -7  <br> 0   |  |  | [ $\begin{array}{r}27 \\ 13 \\ \hline 13 \\ \hline 16\end{array}$ | $\begin{array}{llll}-9 & 9 & -90 \\ -8 & 35 & 33\end{array}$ | ( |
| $52-46$ | ${ }_{239}^{50}{ }^{136}$ |  |  | $\begin{array}{lll}-4 & 31 & -50 \\ -3 & 78 & -73\end{array}$ |  | ${ }^{3}{ }^{73} 88.0$ |  | (1) |  |
| 016 | ${ }_{42}{ }^{2} 2$ | $\begin{array}{llll}-9 & 23 & -19\end{array}$ |  |  |  |  |  | $\begin{array}{llll}-6 & 92 & 91 \\ -5 & 75 & -65\end{array}$ |  |
|  | ( ${ }^{4}$ 9 ${ }^{124}$ |  |  |  | $\begin{array}{rl} \\ -1 & 2077-207 \\ -1 & 315032\end{array}$ | 17.16. | $\begin{array}{lll}-6 & 38 \\ -5 & 00 \\ 080\end{array}$ | -4 60 32 <br> -3   | 39 L |
| ${ }_{2}^{1} 592889$ | 120 |  | $\begin{array}{ccc}-1 & 27 & -33 \\ 0 & 16\end{array}$ | 236 <br> 26 |  | 9 9* | -5 3  <br> -4 36 -37 <br> 10   | -3 53 <br> -2 81 <br> 6 -42 |  |
|  | ${ }_{9}^{9}-20 \times x$ | -3 64 69 <br> -4 125  | 126-122 18 |  | - ${ }^{2} 2930-299$ | 28 L | $\begin{array}{llll}-3 & 32 & 26 \\ -2 & 51 \\ 53\end{array}$ |  | $-8$ |
| ${ }^{3} 828$ |  | -3 233293 | $190-197$ <br> 42 <br> 186 | ${ }_{12}^{12} 9.12$ |  | -9 | -2 31 33 <br> -2 25 -28 <br>  48  |  | ${ }_{-6}^{-7} 99$ |
| 6 36 <br> 7 31 <br>  37 | 0116 |  | ${ }^{4}{ }_{10}{ }^{-36}$ | 3*x |  | $\begin{array}{llll}-8 & 40 & -37 \\ -7 & 15 & 12\end{array}$ |  |  | ${ }_{-4}^{-5} 999^{90} 9$ |
| ( ${ }^{8}$ | ${ }_{96}^{86}{ }_{9}^{-87}$ | (1) | ${ }^{60}{ }_{9}{ }^{-68}$ | 1.4. | (1) | $\begin{array}{lll}-7 & 15 & 12 \\ -6 & 96 & -92 \\ -5 & 20\end{array}$ | $\begin{array}{llll}2 & 9 & -70 \\ 2 & 30 & 30\end{array}$ | 3 38 -33 <br>  26 29 <br>  26  |  |
| 9 30x | $42{ }^{48}$ |  |  |  | - 9 9* | $\begin{array}{llll}-5 & 20 \\ -4 & 12 \\ -780\end{array}$ |  |  |  |
| 02 L | ${ }_{61}{ }_{62}{ }^{62}$ | $\begin{array}{llll} & 18 & 18 & -19\end{array}$ | 9-3*x | $\begin{array}{llll}-5 & 30 & 30\end{array}$ | 23 L | $\begin{array}{lll}-3 & 54 \\ -52\end{array}$ | ${ }_{3}{ }^{13} 9110$ |  |  |
| - 292-358 | $9{ }^{6}$ | 3 612 | 18 L |  | -10 9 20x | $\begin{array}{lll}-2 & 81 \\ -1 & 61 & -62\end{array}$ | 215 L | 3. | $\frac{1}{2} 920{ }^{00 \times}$ |
|  | -80x | 6 | -9 | $\begin{array}{lll}-2 & 30 & -27 \\ -1 & 36 & -60\end{array}$ | $\begin{array}{llll}-9 & 20 & 20 \\ -8 & 23\end{array}$ | (1) ${ }^{0}$ |  |  |  |
| ${ }^{2} 29191215$ |  | ${ }_{9}{ }^{-10 \times}$ | $\begin{array}{lll}-8 & 17 & -17 \\ -7 & 33 & 33\end{array}$ |   <br> 0 36 <br> 0 36 | -8 23 -19 <br> -7 86  <br> 80   | 1 2 $20910{ }^{28}$ | $\begin{array}{llll}-6 & 9 & \\ -5 & 25 & -25^{\circ}\end{array}$ | 50x | ${ }^{3} 88989808$ |
|  | 12 | -70x |  | ${ }^{47}{ }_{9}-4.80$ | -6 23 -24 <br> -3   |  | -4, ${ }_{-3}{ }^{-1}$ | ${ }_{-6} 98$ | 69120 |
| $\stackrel{8}{8}$ ¢ ${ }^{-60}$ | 1 | 13 L | -3 38 36 <br> -4 38 64 <br> 68   | 27-22 |  | $3^{3} \quad 23-29$ |  | -6 9, $960 \times$ | 310 L |
| ? $32{ }^{\circ} 29^{\circ}$ | $2{ }_{2} 1200$ | -10 | -3 <br> 10 |  |  | $\bigcirc{ }^{6} 9{ }^{9}-12^{-4 *}$ |  | -5 36 -31 <br> -6 31  <br> 62   |  |
| ${ }^{-13 *}$ | ${ }^{3} \mathbf{2 0 6 - 1 7 3}$ | -9 | -2 22 12 <br> -1 38  | ${ }_{9}-100$ | -1200 2199 |  | $30-28$ | - ${ }^{-3} 131-136$ |  |
| 036 |  |  |  | 12 |  | 29 L |  | $\begin{array}{lll}-2 & 13 \\ -1 & 1700-180 \\ \\ & 10\end{array}$ | -6 29 -26 <br> -5 17  <br>  -23  |
|  | 26-29 ${ }^{\text {20 }}$ | -6 35 <br> -358  <br> -3 -38 |  |  | ${ }^{2} 10{ }^{10}$ | $-98000 \times 1$ | 9 1*x | - 70.73 |  |
| $\begin{array}{ll}1 & 183-224 \\ \\ 2 & 170-193\end{array}$ |  |  | ${ }^{2} 1233132$ | -6 17 <br> -3 37 <br>  196 | 3 20 13 | $\begin{array}{ll}-7 \\ -7 & 9 \\ 9\end{array}$ | 216 |  | $\begin{array}{lll}-3 & 9 & 104 \\ -2 & 71 & 62\end{array}$ |
| ${ }^{20}{ }^{-26}$ | 013 | -3 -200 -2 $-2007-731$ | ( $\begin{gathered}36 \\ 9\end{gathered}$ |  | 5 -2 0 | -6 25 -28 <br> -5 10  <br> 10   | -5 |  |  |
| ¢ ${ }^{68} 98$ | 163 | - | $8_{8} 27{ }^{22}$ | $\begin{array}{llll}-3 & 33 & 28 \\ -2 & 34 & 38 \\ -6 & 38\end{array}$ |  |    <br> -5 19 19 <br> -4 17  <br>  17  <br> -12   |  | ; ${ }^{38} 9_{-100}^{30}$ |  |
|  | * |  |  | -2 08 <br> 0 0. <br> 0  | - 27 -22 |  | $\begin{array}{llll}-3 & 42 & -40 \\ -2 & 16\end{array}$ | ${ }_{6}^{6}{ }_{9}^{28}{ }^{22} 0 \times$ | ${ }^{2} 123-129$. |
| $9-90$ | ${ }_{-50}^{120}$ | 2222 |  | 68 ${ }^{68}$ |  |  |  |  | ${ }^{29}-2{ }^{9}$ |
| - $2 \cdot 1$ | $59^{9}-3.30 \times$ | 3233233 | 196 | ${ }^{4}$ |  |  | $9-14$ | 3 |  |
| - |  | ${ }_{3}{ }^{129} 9{ }^{128}$ | $-9.190$ | ${ }_{9}^{28}{ }^{26} 0 \times$ | $\begin{array}{cccc}-10 & 19 & 15 \\ -9 & 36 & -34\end{array}$ |  | $\frac{1}{2}$ ¢ ${ }^{\text {c }}$ - $-3 \cdot x$ | -10 ${ }^{-160}$ |  |
|  |  | 16  <br> 12  <br> 12  <br> 8  | $\begin{array}{lll}-8 & 23 & -22 \\ -7 & 32 & 50\end{array}$ | -120 | $\begin{array}{llll} \\ -8 & 36 & 21 \\ -7 & 78\end{array}$ | ${ }^{1} 910 \times 1$ | 3 - -2*x | ${ }^{9}{ }^{28}{ }^{28} 80$ | 311 L |
| 0.099463 $186-147$ | 0 1* | ${ }^{2}$ | -6 35 -41 <br> -5 105  | 126 | -7  7  <br> -6 30   <br> 0    | ; ${ }^{29}{ }^{29} 20 \times 1$ | 217 L |  |  |
|  | 140-226 | -30x |  |  | -5 100 103 <br> -4 136  | ${ }^{9}{ }^{9}-19{ }^{-10 x}$ |  |  | $\begin{array}{llll}-7 & 9 & \\ -6 & 28 & 30\end{array}$ |
| 22 <br> 12 <br> 12 <br> 13 | ${ }^{2} 280$ | $1 \cdot 6$ | -3 82 87 <br> -2 79  <br> 0   | -4 ${ }_{\text {- }}$ |  |  |  |  | -6 28 30 <br> -5 32  <br>  30  |
| ${ }_{9} 96$. | ${ }_{5}^{3} 9{ }^{10}{ }^{10} 0$ | -10 | (er | -3 28 -21 <br> -2 28  <br> 28 -2.  |  | 210 L | $\begin{array}{cccc}-2 & 32 & 32 \\ -1 & 9 & -00\end{array}$ |  |  |
| $9-2 \cdot x$ | 100 | -9, 30x | (1) ${ }^{13}$ |  | (e) | -8 | $0^{9} 90 \times x$ | -1 75 | -3 38 <br> -2 29 <br> -1 -42 |
|  | 015 | -8 9  <br> -7 37 -0 <br> 14   | $2{ }^{1}$ | ${ }_{9}{ }^{-20}$ |  | $-7$ |  | $\begin{array}{ll}73 & 90 \\ 73\end{array}$ | $\begin{array}{llll}-1 & 9 & 130 \\ 0 & 30 & 33^{\circ}\end{array}$ |
| 05 |  | $\begin{array}{llll}-6 & 31 & 39 \\ -5 & 32\end{array}$ |  | 120 | $3^{230-122}$ | -5 $90.4 x$ |  | 27160 | 3939 |
| 051 | ${ }_{9}^{23} 8$ |  | ${ }^{9}-20{ }^{-20}$ | $\begin{array}{lll}23 & 19 \\ 30 & 27\end{array}$ | ${ }^{23}{ }^{-24} 8$ |  |  |  | ${ }^{83}-8.1$ |
| 221-229 | $3^{3} 804{ }^{4}$ | -3 31 | $)^{6}{ }^{23}{ }^{23}-20{ }_{-20 x}$ |  | ${ }_{9}{ }_{\text {10x }}$ | -2 2120112 | $-19080$ | $3{ }^{3} 9.10 x$ | ${ }^{31}-29$ |
| ${ }^{2} 212179.110$ |  | -2 80 -82 <br> -1 24  |  | 175 |  |  | 30 L | ${ }_{7}^{6}{ }^{17}{ }^{-13} 70 \times$ | 2929 |
| -119-99 |  | - $132-139$ |  |  |  | 1 19-10 |  |  |  |
| ${ }^{63}-65$ | - 16 L | ${ }^{2} 12909.190$ | 10 | -3 ${ }^{-3}$ | 231 | ${ }_{2}{ }^{3} 39-36$ | -10 9 - 212 | 36 - |  |
| ¢ ${ }^{-88}$ | $\bigcirc 26-29$ | -1 ${ }^{18}$ | $\begin{array}{llll}-8 & 9 & \\ -7 & 12 & 120 \times\end{array}$ |  |  | ${ }_{23}^{9} 3^{-3 \cdot}$ | -8 030.57 | -10 \% -6\% | -8   <br> -7 15 13 <br> -6   <br> 13   |
| ${ }^{28} 9.19$. | \% - -it: | ${ }^{86} 8.8$ | $\begin{array}{llll}-6 & 12 & 12 \\ -6 & 37 & -99\end{array}$ | ${ }^{0} 23325$ |  | ${ }^{3} 9$ |  |  | -6 90 |
|  | 12. | -2 2 |  | 9 ¢00x | $\begin{array}{llll}-8 & 33 & 36 \\ -7 & 72 & -69\end{array}$ | 7 9, $9 \cdot x$ | -0 211 -203 | -7 ${ }_{-7}$ | -3 22 <br> -6 10 <br>  50 |
| 06 L | ${ }_{7 \times x}^{\text {30x }}$ | 130 | -3 33 | -8*x | -6 19 -19 <br> -5 88  <br> 8   | 212 | +287190 | -6 50 <br> -5 50 <br> 60 -57 | (ers |
| - $301-332$ |  | 9 9-12* | $\begin{array}{ccc}-2 & 43 \\ -1 & 3 \\ 90\end{array}$ | 118 L | - ${ }^{6}$ |  | $\bigcirc 9830$ | - 26.80 | -1 |
|  | 017 L | 3 | -19 ${ }^{-19} 10^{80}$ |  | $\begin{array}{llll}-3 & 33 & 27 \\ -2 & 27 & -11 \\ -1 & 16\end{array}$ |  | 37* |  |  |
|  | ${ }_{2}^{1} 98{ }^{00}$ | -9 |  | $\begin{array}{lll}-2 & 3 & 31 \\ -1 & 9 & -30 x\end{array}$ | -2 18 <br> -1 212 | $\bigcirc{ }_{-6} 9$ | 326 | $\begin{array}{lll}-2 & 72 & -69 \\ -1 & 12 & -67\end{array}$ | $\frac{1}{2} 9^{-120} 8$ |
| 10 <br> 78 <br> 89 | ${ }^{10}$ |  | ${ }_{3}{ }^{2} 98$-100\% | ${ }_{1}^{0} 18{ }_{9}^{18}{ }^{16}$ |  | $\begin{array}{llll}-3 & 33 & -33 \\ -4 & 30 & -28 \\ -23\end{array}$ |  |  |  |
| 28.29 | $4{ }^{18}{ }^{18}$ |  | ${ }_{22}^{72}-21$ |  | ${ }_{2}^{121219}$ | -3 40 | -9 ${ }^{-9}{ }^{200}$ | 1  <br> 2 60 |  |
| 32 27 27 | 0.6 | -6 34 -33 <br> -5 32  <br>  32  <br> 38   | ${ }_{6}{ }^{2} 9000 \times$ | 20 L |  | $\begin{array}{ll}-2 & 27 \\ -1 & 200-102\end{array}$ |  | 3 ${ }^{1}$ |  |
| ${ }^{2}-2 \cdot{ }^{2}$ | 0.23 - |  | -70x | -10 |  | - ${ }^{62} 86$ |  | $\begin{array}{lll}36 & -36 \\ 19 & -15\end{array}$ |  |
| 015 | ${ }^{23} 8.80 \times x$ |  | 1115 |  |  |  |  |  | -7 17 -16 <br> -6 90  <br> -5 20 -50 <br> 0 20  |
|  |  | -1 ${ }^{-1} 399.100$ | $\begin{array}{llll}-8 & 9 \\ -7 & 20\end{array}$ |  | ${ }^{20}$ | 3 37 | $\begin{array}{llll}-3 & 56 & 37 \\ -2 & 261 & 23\end{array}$ | 31 | $\begin{array}{llll} \\ -3 & 20 & 20 \\ -4 & 26 & -20\end{array}$ |
| 2 21909.124 | 10 L |  | $\begin{array}{ll}-7 & 20 \\ -6 & \\ -1000\end{array}$ |  | 26. | ${ }^{3}{ }^{19} 9.20$ | -1 68.73 |  | -3 ${ }^{-3} 10 \times$ |
| ( 55 |  |  |  |  | -9 ${ }^{-1}$ | $4 \cdot x$ |  | -9 $0 \cdot 0{ }^{-120} 0$ |  |
|  |  | $\stackrel{5}{4}^{119-113}{ }^{12}$ | - ${ }^{-3} 122136$ |  | -8 23 30 <br> -7 76  <br> 80   | 212 L | ${ }_{3}^{2123}{ }^{1218} 9.130$ | $\begin{array}{llll}-7 & 9 & -90 \\ -6 & 25 & -20\end{array}$ | $9^{-100} 10$ |
| 72322 | -2 ${ }_{-12}$ |  | -2 $\begin{gathered}\text { 240-235 } \\ -1 \\ 3\end{gathered}$ |  | -6 129818. | $\begin{array}{ll}-8 \\ -7 & 9 \\ -7 & -80 x \\ 20 x\end{array}$ |  |  | ${ }^{\text {a }}$ - ${ }^{1210}$ |
|  |  | ${ }_{9}^{8} 88.8$ | - 1000.91 | 21 | ${ }_{-9}^{-3} 122^{9} 129^{\circ}{ }^{\circ}$ | ${ }_{-6}^{-7} 98$ |  | $\begin{array}{lll}-3 & 53 & -4 \\ -3 & 72\end{array}$ | $3^{3} 9.950$ |
|  |  | ${ }^{60} \times$ | ${ }^{2} 99^{9} 9{ }^{-9}{ }^{60 x}$ |  | -3 93 -89 <br> -2 68  <br>  68  |  |  | $\begin{array}{llll}-2 & 57 & 48 \\ -1 & 21 & -18\end{array}$ |  |
|  |  | 16 L | ( ${ }^{24}{ }_{9}{ }_{-30}^{22} \times$ |  |  |  | ${ }^{-3}$ | (1) | 310 |
|  | 12 |  | ${ }_{9}^{17}{ }_{-12}^{12}$ | -6 99.88 | 2 $37-40$ |  | 3 | -90* | $\begin{array}{llll}-6 & 16 & 33 \\ -5 & 16 & -10\end{array}$ |
| 2 11 <br> 3 20.0 <br>  225 | -10 9 ${ }^{10}$ | $\begin{array}{llll}-8 & 9 & 10 \\ -7 & 39 & -37 \\ -8 & 9\end{array}$ | -120 |  | $\begin{array}{llll}2 & 22 & 19 \\ 3 & 23 & 19 \\ & 23 & 17\end{array}$ |  | ${ }_{-9}^{10} 98$ | -20x | -6 9 50 <br> 0   |
|  17  <br> 5 25 17 <br> $0 \times$   |  | ${ }^{-6}$ | ${ }^{2} 212 \mathrm{~L}$ | (1) |  | 2 33  <br>  33  <br>  3 30 | -9, ${ }_{-7}$ | ${ }^{x}$ |  |
| 3 27 <br>  27 <br> 7 27 | -7 53 32 <br> -6 36  <br>  31  |  | -7 20 <br> -6 -19 <br>  9 | $\begin{array}{ccc}-1 & 32 & 33 \\ 0 & 324 & 3 \\ 0 & 388\end{array}$ |  |  |  | -0*x | (1) |
|  |  | -2 $180-196$ <br> -1 316 <br> 1826  | -3 57 <br> -4 9 |  | ${ }_{100}$ | ¢ ${ }_{60 \times}$ |  | 38 | ${ }^{3} 9{ }^{9}-120^{\circ}$ |
| - 1715 |  | (1) |  | 2 1200 <br> 3 123 <br>  129 | 27 L | 223 |  |  | $9{ }_{9}{ }^{60}{ }^{\text {a }}$ |
| $0 \cdot 6$ | $\begin{array}{ll}-2 & 390-043 \\ -1 & 329-409\end{array}$ | 1  <br> 2 308 <br> 2 85 | -1 | ; ${ }^{18}{ }^{28}{ }^{20} 0$ |  | - ${ }^{5}$ 9 50x |  |  |  |
|  | - |  |  | ${ }_{20} 8^{-30 \times}$ | -8 0.70 | -7 9 $30 x$ <br> -6 9 $-50 \times$ <br> -50 30  |  |  |  |
|  |  | ${ }^{33}{ }^{3} 3$. | ${ }_{9}^{26}{ }_{-9}^{-29}$ | ${ }_{3}^{24}{ }^{24}{ }^{-19}$ |  |  | $\begin{array}{llll}2 & 184 \\ 3 & 183 & 385\end{array}$ | -5 18 <br> -4 -13 <br> 80  | $\begin{array}{llll}-6 & 30 & -23^{30 x}\end{array}$ |
|  |  | $\begin{array}{rrr}34 & -30 \\ 12 \\ 12\end{array}$ | 29 |  |  | $\begin{array}{lll}-3 & 27 \\ -2 & 29 \\ -290\end{array}$ | - 1198129 | - ${ }_{\text {- }}$ |  |
|  | ${ }_{9}^{128-122} 3$ | $9{ }_{9}$ | ${ }_{9}^{27}{ }^{22}{ }_{20}$ | 226 | $-4$ | -2 9 <br> -2 29 <br> 20  | 5119 |  |  |
| 7 12-8 | $6 \rightarrow 4.42$ |  |  | -10, -60x |  | ${ }^{\circ} 9{ }^{\circ} \mathrm{x}$ | 73331 | - 28 -27 | 1820 |

neglected, and positional and isotropic thermal parameters were refined for nonhydrogen atoms. In the later stages ring hydrogen atoms were introduced in expected positions but not refined. After shifts in successive cycles had become small in comparison to standard deviations, the agreeement factor

$$
R=\Sigma\left|F_{\mathrm{o}}-F_{\mathrm{c}}\right| / \Sigma F_{\mathrm{o}}
$$

excluding unobserved reflections was 0.15 . A three-
dimensional Fourier electron-density synthesis was cal culated with program MIFRI. ${ }^{13}$ All hydrogen atom: were found with fairly well-defined peaks at roughl! the expected positions, except the carbonyl hydroger $(\mathrm{H})$ which was on a rather poorly defined peak. Thi peak was roughly on a straight line between its as sociated oxygen atom and the double-bonded oxygen or the centrosymmetrically related molecule, so as tc
(13) D. P. Shoemaker and W. G. Sly', Acta Cryst., 14, 552 (1961).

| foos feal | －foess fat | 18085 PCaL -4 |  |  |  | Leose ccal <br> -630 <br> -32 | Leobs fcal | $L$ FOAS FCAL $2930 x$ | $\begin{aligned} & \text { Lfoss feal } \\ & \because: \therefore: \quad \therefore \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  | $2,8$ |  |
| ${ }_{13}{ }^{3}{ }^{\text {a }}$ | （ear | （1） |  |  |  |  |  |  |  |
| 16 L |  |  |  | （ |  | （ex |  |  | －7 ${ }_{\text {－7 }}^{0}$ |
| －3 ${ }_{\text {a }}$ |  | ${ }^{3}{ }_{9}^{22} 820.4$ |  |  |  |  |  | －${ }_{\text {－}}^{\text {－}}$ |  |
| $\mathrm{Co}_{-2}^{2}$ |  |  |  | －8 9－30x | （ | 612 L |  |  |  |
| （1） |  |  | （1） |  |  |  | （eater | ， |  |
| $2{ }^{2}-10 \times$ |  | （ex |  |  |  | （eater | $\stackrel{9}{9} 9{ }_{9}^{-200}$ | －7 ，－30x | －6 ，30x |
|  |  |  |  |  | － | － | ＞3 | －${ }_{\text {－}}^{\text {－}}$ |  |
|  | ， |  |  | （erser | 边 |  | －8， |  |  |
|  |  |  |  |  |  |  |  |  |  |
| （10 |  | － |  | ， |  |  |  |  |  |
|  | －${ }_{\text {－}}^{\text {－}}$ | ${ }_{-7}^{-7}{ }_{-6}^{13} 96$ |  |  | （eack | － | （en | －6－－2＊x |  |
|  |  | － |  | －${ }_{\text {－}}$ |  |  | 2 9－ 0 |  |  |
| ${ }_{9}^{18} 9$ | ${ }^{\circ}$ |  | $\xrightarrow{-1} 128-1190 \times$ | －$-3.12{ }^{16}$ | ${ }^{-3}$ | －13 |  | －3 ${ }_{\text {－}}$ |  |
|  |  |  |  |  |  |  | －9， $20.11^{10 \times}$ | （ex | －． |
|  |  | ${ }^{2}$ |  |  | \％${ }_{\text {d }}$ | －2 ${ }_{-1}$ | －${ }_{\text {－}}^{\text {－}}$ | 79. |  |
| （eater | 27 | ${ }_{9}{ }^{-3} 5$ |  |  |  |  | －3 ${ }_{\text {－}}$ |  |  |
|  |  | －5 ${ }^{\text {a }}$ 10x |  | $\because 810$ | －3L |  | （ex | （e） | ，－6＊x |
|  | －7 |  | － |  | －：${ }_{\text {－}}$ | ${ }^{-2} 0 \cdot 0 \cdot x$ | － | － | ${ }^{3} 5$ |
|  | $\xrightarrow{-5}{ }_{9}^{20} 9$ |  |  |  |  | $9{ }^{13}{ }^{\circ}$ |  |  | －0，${ }_{\text {－}}^{0}$ |
| O 10.3 |  |  | －2 39 | － | －${ }^{-6}$ | 1 |  |  |  |
|  |  | $2910 \times$ |  | （ex |  |  | － |  | －2 ${ }_{-1}$ |
|  | \％${ }_{2}$ |  |  |  | － | －6 ${ }^{\circ}$ | ${ }_{-3}^{-3}$ |  | 0 |
| ${ }_{7}^{33}{ }^{-28} 6 \times$ x | 成 |  |  |  |  | $\underbrace{-3}_{\text {－}}$ | －2，${ }_{-1}$ |  | －${ }_{-3}$ |
| －2L | 18.19 |  |  |  |  | （ersor | （ ${ }_{\text {x }}^{\text {¢ }}$ | －6 ，－3＊x | － |
|  |  | ${ }_{24}{ }^{26}$ |  |  | 60t |  |  |  |  |
| －8，${ }_{\text {－}}$ |  | － 20 L |  |  |  |  |  |  |  |
| －${ }_{\text {－}}^{5}$ |  |  |  | $\frac{1}{2}$ ；－3：＊ | （1） |  |  |  |  |
|  |  | －2 | －3 ${ }^{-36}$ | 310 L |  |  |  |  |  |
|  |  |  | （tar |  | －2．${ }_{\text {－}}$ |  |  |  |  |
|  |  | －10－ 0 |  |  | ${ }^{\frac{1}{2}} \stackrel{20}{20} 98$. |  |  |  |  |
| 边 | ； $\mathrm{ii}:$ | ${ }_{-10}^{-10} 808$ |  |  | ${ }_{3}^{2}{ }^{2} 9$ |  | Mozes | crions．ratue |  |
| 价 |  |  | ${ }^{\text {S }} 16$－ 16 | $\bigcirc{ }_{i} ;$ | 1 |  |  | Sens |  |
|  | ${ }^{5} 180$ | － | ${ }^{1}$ | 525 | $\because 8$ |  | REF1NE ERROR |  |  |
| －3 5 | －9 | ${ }_{30}{ }_{30}{ }^{-27}$ |  |  | ${ }_{-6}{ }_{-6}{ }^{23}$ |  | Mobservo | Crions om |  |
|  | －i ${ }_{\text {－}}$ | 316 |  |  |  |  | sus | ABn |  |
| －${ }_{\text {－}}$ |  |  |  |  |  |  | Hor ${ }^{\text {anc }}$ | ir |  |
| （ers |  | 边 |  |  |  |  | IThe Pran | Ster |  |
| $\stackrel{-598}{-5} 9$ |  | －6 20.30 | ${ }^{-1}$ | －-2 | 3 9，－5．x |  | Revele |  |  |
| －305 |  |  |  | － | 60 L |  |  | 边 |  |
|  |  | － |  |  |  |  | （tater | NLCAL |  |
| ${ }^{2}$ |  |  | ${ }^{\circ} 9$ |  |  |  |  |  |  |
|  |  | 价 | $5{ }^{3} \mathrm{~L}$ |  | （ers |  |  |  |  |
|  |  |  | － |  | － |  |  |  |  |
|  |  | 322 | － |  |  |  |  |  |  |
|  |  | ${ }_{-9}^{-10} 9$ |  | －${ }_{\text {cos }}$ | －${ }^{\circ}$ |  |  |  |  |
| －8，${ }^{-7}{ }^{\text {a }}$ | －2 ${ }_{-1} \stackrel{9}{9}$ | $\xrightarrow{-9}$ ，iox |  | ${ }_{2}^{2}$ | －7 |  |  |  |  |
|  | － | －670 <br> -30 | （ex |  |  |  |  |  |  |
|  | － |  | －${ }^{2}$ | 2 L |  |  |  |  |  |
|  | ${ }_{9}^{20}$ |  |  |  |  |  |  |  |  |
| （tale |  |  |  |  |  |  |  |  |  |
| ${ }^{\text {a }}$ | ${ }^{-9} 8$ | 边 | ${ }_{-6}^{-7}$ |  |  |  |  |  |  |
|  | （er | ${ }_{17}{ }_{19}$ |  |  |  |  |  |  |  |

suggest an $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ hydrogen bond of length $2.6 \AA$ ． The hydrogen peaks were not sufficiently good to merit individual positional refinement but collectively they suggested small shifts in their relation to the ring carbon atoms which were made before continued refinement． Strong indications of anisotropic thermal motion of the nonhydrogen atoms were also shown by the electron density function．

Further least－squares refinement was done on an IBM 7094 computer using the program ORFLS．${ }^{14}$
（14）W．R．Busing，K．O．Martin，and H．A．Levy，＂ORFLS，a For－

All positional and anisotropic thermal parameters for all nonhydrogen atoms were refined with the full normal equation matrix．Ring hydrogen positions were assigned so that each $\mathrm{C}-\mathrm{H}$ bond was $1.08 \AA$ ． in length and was coplanar with the adjacent ring bonds，and so that the ratio of the angle made with the double bond to that made with single bond was a constant，taken to be 1.062 ．The carbonyl hydrogen atom H was assigned a position at a distance of 0.96
tran Crystallographic Least－Squares Program，＂Oak Ridge National Laboratory，ORNL－TM－305 Aug． 1962.


Figure 1. The crystal structure as viewed along the crystallographic $b$ axis ( $y$ going into the paper). Molecules at the left edge of the unit cell outline are omitted.
$\AA$. from its oxygen atom, $O(2)$, and as close as possible to the straight line connecting $\mathrm{O}(2)$ with $\mathrm{O}(1)$ of the centrosymmetrically related molecule, subject to an imposed $\mathrm{C}(9)-\mathrm{O}(2)-\mathrm{H}$ angle of $105^{\circ}$. Hydrogen atoms were given thermal parameters computed from an arbitrarily assigned isotropic temperature factor $B=$ 5.0 in the usual units of $(0.5 \AA .)^{2}$. Weights were assigned to the structure factors by the method of Hughes. ${ }^{11}$ In the final stages, unobserved reflections were included in refinement where calculated values of structure factors exceeded the assigned lower limits of observability. A few reflections were omitted from the refinement because of extinction or suspicion of highly abnormal error; these and other special cases are indicated in the structure factor table (Table III) and its footnotes. Refinement was continued until parameter shifts were small in comparison to the indicated standard deviations. The final value of the agreement factor $R$, including all unobserved reflections used in the last refinement cycle, was 0.101 .
The final values of the atomic coordinates are given in Table I, and the bond distances and interbond angles calculated from them are shown in Figure 2. In Table II are given the thermal parameters ( $\beta_{i j}$ in the temperature factor expression $\exp -\left(\beta_{11} h^{2}+\beta_{22} k^{2}+\right.$ $\left.\beta_{33^{2}}{ }^{2}+2 \beta_{12} h k+2 \beta_{13} h l+2 \beta_{23} k l\right)$. Also given are vibration amplitudes ( $U$ ) in Ångstrom units for the three principal axes of the thermal ellipsoid, and also the orientations of these axes (direction cosines $u$, $\nu$, and $w$ ). The distances, angles, and ellipsoid parameters were computed by the IBM 7094 with programs DISTAN and VIBELL. ${ }^{15}$ The observed and final calculated structure factors are given in Table III.
(15) D. P. Shoemaker, "DISTAN Criptallographic Bond Distance, Bond Angle, and Dihedral Angle Computer Program," M.I.T., April 1963; D. P. Shoemaker and R. C. Srivastava, "VIBELL Anisotropic


Figure 2. The crystal structure as viewed perpendicular to the crystallographic ( 001 ) plane ( $z$ coming at an angle out of the paper). The molecule at upper left is the same one as is labeled in Figure 1. The two molecules forming one dimer are labeled with angles and distances (in Angstrøm units). The molecule at upper right is the one which corresponds to parameter values given in Table I. The atom circles outline stereographic projections of the poles of the principal thermal parameters of the nonhydrogen atoms. The black circle with white dot represents the axis of strongest thermal motion (3), the open circle with black dot represents the next strongest (2), and the open circle represents with its center the least strong (1). The diameters of these symbols are proportional to the respective estimated r.m.s. vibration amplitudes.

## Description of the Structure

The crystal structure is shown in two projections in Figures 1 and 2. The molecules are clearly present as hydrogen-bonded dimers, as in benzoic acid ${ }^{16}$ and in many other crystalline carboxylic acids. The COT ring is nearly perpendicular to the $c$ axis of the crystal; packing is good, the COT rings being about $4 \AA$. apart in the $c$ direction. Interatomic distances and bond angles shown in Figure 2 are as calculated directly from the lattice constants and positional parameters; they were not corrected for thermal motion since no sound basis for making such corrections seemed apparent.
The COT ring has the tub form and conforms very closely with $D_{2 d}$ symmetry. The standard error in a positional parameter of an atom, as computed from least-squares residuals, is about $0.005 \AA$. for a carbon atom and a little less for an oxygen atom; this leads to an estimated standard error of $0.007 \AA$. in a $\mathrm{C}-\mathrm{C}$ interatomic distance and $0.5^{\circ}$ in a $\mathrm{C}-\mathrm{C}-\mathrm{C}$ angle. It would seem wise to raise our estimates to perhaps $0.010 \AA$. and $0.7^{\circ}$ in view of possible systematic errors

[^1]Table IV. Average Values of COT Ring Parameters

| Ref. | Substance | Method | Double bond, <br> $\AA$. | Single bond, <br> $\AA$ | Angle, <br> degrees |
| :---: | :--- | :--- | :---: | :---: | :---: |
| This work | COT acid | X-Ray | $1.322 \pm 0.005$ | $1.470 \pm 0.005$ | $126.4 \pm 0.4$ |
| W, S, $\mathbf{S}^{27}$ | CaCOT | X-Ray | 1.337 | 1.464 | 126.3 |
| K, F, $\mathbf{M}^{8}$ | COT | X-Ray | $(1.34)$ | $(1.54)$ | $(125)$ |
| B, H, H ${ }^{7}$ | COT | E.d. | $1.334 \pm 0.001$ | $1.462 \pm 0.001$ | $126.46 \pm 0.23$ |

arising from the arbitrary assignment of weights and hydrogen positions, as well as uncertainties in the lattice parameters. The four ring double-bond distances show a maximum deviation of $0.012 \AA$. from the average of $1.322 \AA$. , and the four ring single-bond distances show a maximum deviation of $0.020 \AA$. from their average of $1.470 \AA$. The eight ring angles average to $126.4^{\circ}$, with a maximum deviation of $1.2^{\circ}$ from the average. It appears, then, that the small apparent deviations of ring carbon atoms from a strict $D_{2 d}$ configuration are not significant.

The dihedral angles between ring bond planes intersecting in a double bond have a maximum of $1.29^{\circ}$ and an average of $0.77^{\circ}$, indicating a high degree of planarity in the double bonds. The dihedral angles between planes intersecting in a single bond average $57.12^{\circ}$ and have a total spread of $1.26^{\circ}$.
In Table IV the average COT ring parameters obtained in this work are compared with those published previously and with values obtained in as yet unpublished work on calcium 2,4,6,8-cyclooctatetraene-1,2dicarboxylate dihydrate ("CaCOT"). ${ }^{17}$ The standard deviations given for our averages are those for individual values divided by $\sqrt{4}$, but the values are still possibly subject additionally to subtle systematic errors resulting from somewhat arbitrary placement of ring hydrogens. Such possible errors might account in part for the disagreements with the electron diffraction results, but they cannot easily account for the disagreements with the CaCOT results since in these the hydrogen contributions were assigned in a substantially identical way (except for somewhat different temperature factors). It would appear that these differences are possibly significant although no explanation is readily apparent.

The bond to the carboxyl group is bent away from the plane of the double bond so as to be more nearly parallel with the mean plane of the COT ring; the three bond-plane dihedral angles are roughly the same and average $6.1^{\circ}$. The carboxyl group itself is very nearly

[^2]planar (the dihedral angles between bond planes in the carboxyl group do not exceed $0.55^{\circ}$ ) and is closely coplanar (within $2.5^{\circ}$ ) with the adjacent double bond in the ring. The $\mathrm{C}-\mathrm{C}, \mathrm{C}=\mathrm{O}$, and $\mathrm{C}-\mathrm{O}$ distances and the $\mathrm{C}-\mathrm{C}=\mathrm{O}, \mathrm{C}-\mathrm{C}-\mathrm{O}$, and $\mathrm{O}=\mathrm{C}-\mathrm{O}$ bond angles are in reasonable agreement with respective values of 1.48 A., $1.24 \AA ., 1.29 \AA ., 122^{\circ}, 118^{\circ}$, and $122^{\circ}$ in benzoic acid, ${ }^{16}$ and with $1.46 \AA ., 1.24 \AA ., 1.33 \AA ., 123^{\circ}$, $117^{\circ}$, and $120^{\circ}$ in salicylic acid. ${ }^{18}$ The $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ hydrogen bond distance between oxygen pairs in the dimer, $2.604 \AA$., is in the range covered by such distances in typical carboxylic acid crystals such as benzoic acid (dimer), $2.64 \AA .{ }^{16}$ acetic acid (chain), 2.61 A., ${ }^{19}$ and formic acid (chain), $2.58 \AA .{ }^{20}$
The molecule shows its strongest thermal motions roughly normal to the plane of the ring (Table II, Figure 2). Only on $C(6)$ is this apparently not the case, but the difference between the values given for $U_{2}$ and $U_{3}$ is presumably smaller than the uncertainties in these qualities, and the true order may in fact be reversed. The largest vibrations are on the carboxyl oxygens (corresponding presumably in part to a libration about the $C(1)-C(9)$ bond) and on the ring carbon atoms farthest from the carboxyl group (corresponding presumably in part to a wagging of the ring). The actual r.m.s. magnitudes of the thermal motion are more of relative than of absolute significance, since systematic errors in the temperature factor magnitudes arise from visual estimation of intensities (due to variable spot shape) and uncorrected absorption.

Acknowledgments. We wish to express our appreciation to Professor A. C. Cope for providing us with a specimen of COT acid, and to Professor Ray Pepinsky for use of XRAC without charge. We also wish to thank our sources of support. ${ }^{1.2}$ Dr. Ronald Chandross and Mr. R. Nacciarone assisted with the calculations, and Dr. K. Seff prepared the illustrations.

[^3]
[^0]:    (1) This work was done in part under a Grant-in-Aid from E. I. du Pont de Nemours Co., and in part under Grant A2400 (GM-10850) from the National Institutes of Health. Computations wene done in part on XRAC at Pennsylvania State University and in part at the M.I.T. Computation Center.
    (2) Participation in this work was sponsored by the Foreign Student Summer Project, Massachusetts Institute of Technology.
    (3) A. C. Cope, M. Burg, and S. W. Fenton, J. Am. Chem. Soc., 74, 173 (1952).
    (4) E. R. Lippincott, R. C. Lord, and R. S. MacDonald, ibid., 73, 3370 (1951).
    (5) K. Hedberg and V. Schomaker, Abstracts, American Chemical Society Meeting, San Francisco, Calif., March 1949.
    (6) I. L. Karle, J. Chem. Phys., 20, 65 (1952).
    (7) O. Bastiansen, L. Hedberg, and K. Hedberg, ibid., 27, 1311 (1957).
    (8) H. S. Kaufman, I. Fankuchen, and H. Mark, Nature, 161, 165 (1948).
    (9) H. Kindler and D. P. Shoemaker, Abstracts, American Chemical Society Meeting, Los Angeles, Calif, March 1953.

[^1]:    Thermal Parameter Interpreting Program," M.I.T., June 1963. Fortran decks are available from the first-named author on request
    (16) G. A. Sim, J. M. Robertson, and T. H. Goodwin, Acta Cryst., 8, 157 (1955).

[^2]:    (17) D. A. Wright, K. Seff, and D. P. Shoemaker, to be published.

[^3]:    (18) W. Cochran, Acta Cryst., 6, 260 (1953).
    (19) R. E. Jones and D. H. Templeton, ibid., 11, 487 (1958).
    (20) F. Holtzberg, B. Post, and I. Fankuchen, ibid., 6, 127 (1953)

